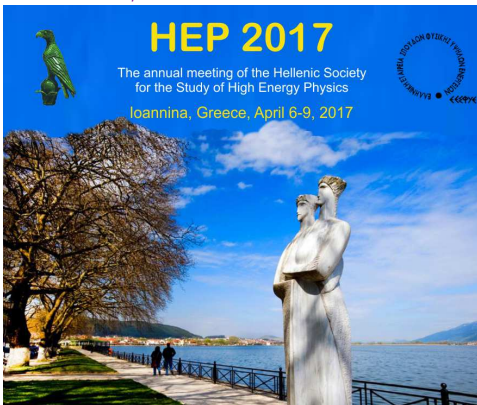


Aspects of string phenomenology and scale hierarchies

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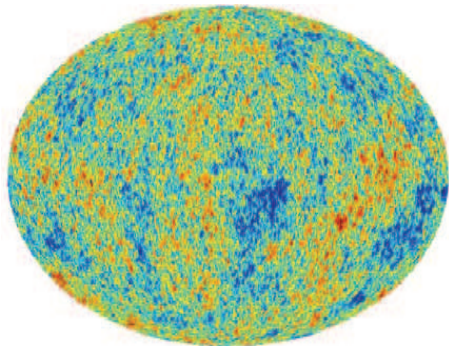


Main predictions → inspirations for BSM physics

- Spacetime supersymmetry but arbitrary breaking scale
- Extra dimensions of space six or seven in M-theory
- Brane-world description of our Universe
matter and gauge interactions may be localised in less dimensions
- Landscape of vacua
- ...

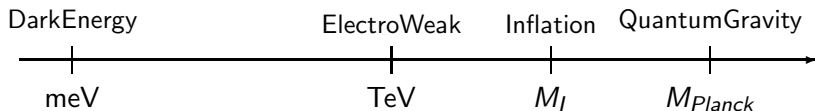
Connect string theory to the real world

- Is it a tool for strong coupling dynamics or a theory of fundamental forces?
- If theory of Nature can it describe both particle physics and cosmology?

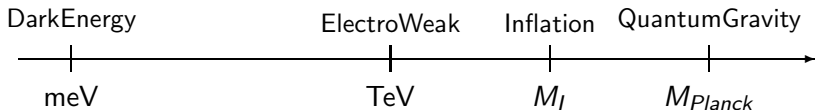


Problem of scales

- describe high energy (SUSY?) extension of the Standard Model
unification of all fundamental interactions
 - incorporate Dark Energy
simplest case: infinitesimal (tuneable) +ve cosmological constant
 - describe possible accelerated expanding phase of our universe
models of inflation (approximate de Sitter)
- ⇒ 3 very different scales besides M_{Planck} :



Problem of scales



① they are independent

② possible connections

- M_I could be near the EW scale, such as in Higgs inflation

but large non minimal coupling to explain

- M_{Planck} could be emergent from the EW scale

in models of low-scale gravity and TeV strings

What about M_I ? can it be at the TeV scale?

Can we infer M_I from cosmological data?

I.A.-Patil '14 and '15

- connect inflation and SUSY breaking scales

impose independent scales: **proceed in 2 steps**

① SUSY breaking at $m_{SUSY} \sim \text{TeV}$

with an infinitesimal (tuneable) positive cosmological constant

Villadoro-Zwirner '05

I.A.-Knoops, I.A.-Ghilenca-Knoops '14, I.A.-Knoops '15

② Inflation connected or independent? [15] [23]

Toy model for SUSY breaking

Content (besides $N = 1$ SUGRA): one vector V and one chiral multiplet S
with a shift symmetry $S \rightarrow S - ic\omega \leftarrow$ transformation parameter

String theory: compactification modulus or universal dilaton

$$s = 1/g^2 + ia \leftarrow \text{dual to antisymmetric tensor}$$

Kähler potential K : function of $S + \bar{S}$

$$\text{string theory: } K = -p \ln(S + \bar{S})$$

Superpotential: constant or single exponential if R-symmetry $W = ae^{bS}$

$$\int d^2\theta W \text{ invariant}$$

$$b < 0 \Rightarrow \text{non perturbative}$$

can also be described by a generalized linear multiplet [11]

Scalar potential

$$\mathcal{V}_F = a^2 e^{\frac{b}{l}} l^{p-2} \left\{ \frac{1}{p} (pl - b)^2 - 3l^2 \right\} \quad l = 1/(s + \bar{s})$$

Planck units

- $b > 0 \Rightarrow$ SUSY local minimum in AdS space with $l = b/p$
- $b \leq 0 \Rightarrow$ no minimum with $l > 0$ ($p \leq 3$)

but interesting metastable SUSY breaking vacuum when R-symmetry is gauged by V allowing a Fayet-Iliopoulos (FI) term:

$$\mathcal{V}_D = c^2 l (pl - b)^2 \quad \text{for gauge kinetic function } f(S) = S$$

- $b > 0$: $\mathcal{V} = \mathcal{V}_F + \mathcal{V}_D$ SUSY AdS minimum remains
- $b = 0$: SUSY breaking minimum in AdS ($p < 3$)
- $b < 0$: SUSY breaking minimum with tuneable cosmological constant Λ

minimisation and spectrum

Minimisation of the potential: $V' = 0$, $V = \Lambda$

In the limit $\Lambda \approx 0$ ($p = 2$) \Rightarrow [17]

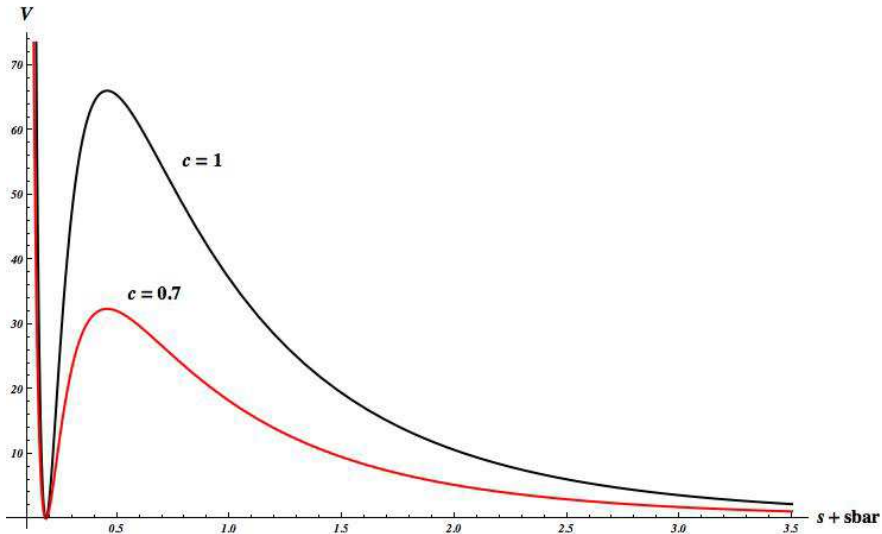
$$b/l = \rho \approx -0.183268 \quad \Rightarrow \langle l \rangle = b/\rho$$

$$\frac{a^2}{bc^2} = 2 \frac{e^{-\rho}}{\rho} \frac{(2-\rho)^2}{2+4\rho-\rho^2} + \mathcal{O}(\Lambda) \approx -50.6602 \quad \Rightarrow c \propto a$$

Physical spectrum:

massive dilaton, $U(1)$ gauge field, Majorana fermion, gravitino

All masses of order $m_{3/2} \approx e^{\rho/2} l a \leftarrow$ TeV scale



[15]

Properties and generalizations

- Metastability of the ground state: extremely long lived

$$l \simeq 0.02 \text{ (GUT value } \alpha_{GUT}/2) m_{3/2} \sim \mathcal{O}(\text{TeV}) \Rightarrow$$

$$\text{decay rate } \Gamma \sim e^{-B} \text{ with } B \approx 10^{300}$$

- Add visible sector (MSSM) preserving the same vacuum

matter fields ϕ neutral under R-symmetry

$$K = -2 \ln(S + \bar{S}) + \phi^\dagger \phi \quad ; \quad W = (a + W_{MSSM}) e^{bS}$$

\Rightarrow soft scalar masses non-tachyonic of order $m_{3/2}$ (gravity mediation)

- Toy model classically equivalent to [7]

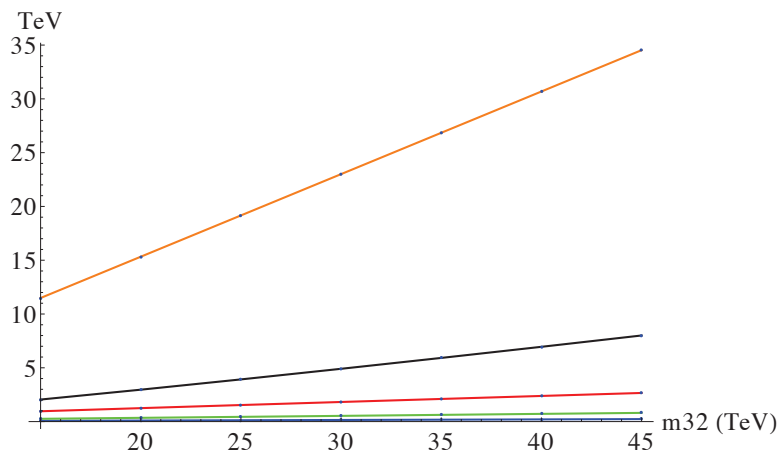
$$K = -p \ln(S + \bar{S}) + b(S + \bar{S}) \quad ; \quad W = a \quad \text{with } V \text{ ordinary } U(1)$$

- Dilaton shift can be identified with $B - L \supset$ matter parity $(-)^{B-L}$

Properties and generalizations

- R-charged fields needed for anomaly cancellation
- A simple (anomaly free) variation: $f = 1$ and $p = 1$
tuning still possible but scalar masses of neutral matter tachyonic
possible solution: add a new field Z in the 'hidden' SUSY sector
 \Rightarrow one extra parameter
- alternatively: add an S -dependent factor in Matter kinetic terms
$$K = -\ln(S + \bar{S}) + (S + \bar{S})^{-\nu} \sum \Phi \bar{\Phi} \quad \text{for } \nu \gtrsim 2.5$$
 \Rightarrow similar phenomenology
- distinct features from other models of SUSY breaking and mediation
- gaugino masses at the quantum level
 \Rightarrow suppressed compared to scalar masses and A-terms

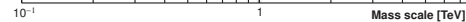
Typical spectrum



The masses of sbottom squark (yellow), stop (black), gluino (red), lightest chargino (green) and lightest neutralino (blue) as a function of the gravitino mass. The mass of the lightest neutralino varies between ~ 40 and 150 GeV [6]

Model	e, μ, τ, γ	Jets	E_{T}^{miss}	$\int L d(\ln^{-1})$	Mass limit	$\sqrt{s} = 7, 8$ TeV	$\sqrt{s} = 13$ TeV	Reference	
Inclusive Searches	MSUGRA/CMSSM	$0.3 e, \mu/1-2$	2-10 jets/3 b	Yes	20.3	$\tilde{\chi}_1^0$	1.85 TeV $m(\tilde{\chi}_1^0)=m(\tilde{g})$	1507.05525	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	13.3	$\tilde{\chi}_1^0$	1.35 TeV $m(\tilde{\chi}_1^0)=200$ GeV, $m(\tilde{g})=m(\tilde{g})$	ATLAS-CONF-2016-078	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$ (compressed)	mono-jet	1-3 jets	Yes	3.2	$\tilde{\chi}_1^0$	608 GeV $m(\tilde{\chi}_1^0)=5$ GeV	1604.07773	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	13.3	$\tilde{\chi}_1^0$	1.86 TeV $m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-078	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0 \rightarrow q\bar{q}W\tilde{\chi}_1^0$	0	2-6 jets	Yes	13.3	$\tilde{\chi}_1^0$	1.83 TeV $m(\tilde{\chi}_1^0)=400$ GeV, $m(\tilde{\chi}_1^0)=0.5(m(\tilde{\chi}_1^0)+m(\tilde{g}))$	ATLAS-CONF-2016-078	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$	$3 e, \mu$	4 jets	-	13.2	$\tilde{\chi}_1^0$	1.7 TeV $m(\tilde{\chi}_1^0)=400$ GeV	ATLAS-CONF-2016-037	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}WZ\tilde{\chi}_1^0$	$2 e, \mu$ (SS)	0-3 jets	Yes	13.2	$\tilde{\chi}_1^0$	1.6 TeV $m(\tilde{\chi}_1^0) < 500$ GeV	ATLAS-CONF-2016-037	
	GMSB (if NLSP)	$1-2 \tau, 0-1 \ell$	0-2 jets	Yes	3.2	$\tilde{\chi}_1^0$	2.0 TeV	1607.08979	
	GGM (bino NLSP)	2γ	-	-	3.2	$\tilde{\chi}_1^0$	1.65 TeV $r(\text{NLSP}) > 0.1$ mm	1606.09150	
	GGM (higgsino-bino NLSP)	γ	1 b	Yes	20.3	$\tilde{\chi}_1^0$	1.37 TeV $r(\text{NLSP}) > 0.1$ mm, $\mu=0$	1507.05493	
	GGM (higgsino-bino NLSP)	γ	2 jets	Yes	13.3	$\tilde{\chi}_1^0$	1.8 TeV $m(\tilde{\chi}_1^0)=680$ GeV, $r(\text{NLSP}) > 0.1$ mm, $\mu=0$	ATLAS-CONF-2016-066	
	GGM (higgsino NLSP)	$2 e, \mu$ (Z)	2 jets	Yes	20.3	$\tilde{\chi}_1^0$	900 GeV $m(\text{NLSP}) > 430$ GeV	1503.03290	
Gravitino LSP	0	mono-jet	Yes	20.3	$F^{1/2}$ scale	865 GeV $m(\tilde{G}) > 1.8 \times 10^{-11} eV, m(\tilde{g})=m(\tilde{g})=1.5$ TeV	1502.01518		
$\tilde{\chi}_1^0$ gen. & med. prod.	$\tilde{g}, \tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$	0	3 b	Yes	14.8	$\tilde{\chi}_1^0$	1.89 TeV $m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-052	
	$\tilde{g}, \tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$	$0-1 e, \mu$	3 b	Yes	14.8	$\tilde{\chi}_1^0$	1.89 TeV $m(\tilde{\chi}_1^0)=0$ GeV	ATLAS-CONF-2016-052	
	$\tilde{g}, \tilde{g} \rightarrow b\bar{b}\tilde{\chi}_1^0$	$0-1 e, \mu$	3 b	Yes	20.1	$\tilde{\chi}_1^0$	1.37 TeV $m(\tilde{\chi}_1^0)=300$ GeV	1407.0600	
$\tilde{\chi}_1^0$ gen. squarks direct production	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$	0	2 b	Yes	3.2	\tilde{b}_1	840 GeV $m(\tilde{\chi}_1^0)=100$ GeV	1606.08772	
	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\tilde{\chi}_1^0$	$2 e, \mu$ (SS)	1 b	Yes	13.2	\tilde{b}_1	325-685 GeV $m(\tilde{\chi}_1^0)=150$ GeV, $m(\tilde{t}_1)=m(\tilde{t}_1)+100$ GeV	ATLAS-CONF-2016-037	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$	$0-2 e, \mu$	1-2 b	Yes	4.7/13.0	\tilde{t}_1	200-720 GeV $m(\tilde{\chi}_1^0)=1$ GeV	1209.2102, ATLAS-CONF-2016-077	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$ or \tilde{t}_1^*	$0-2 e, \mu$	0-2 jets/1-2 b	Yes	4.7/13.3	\tilde{t}_1	90-198 GeV $m(\tilde{\chi}_1^0)=1$ GeV	1506.08616, ATLAS-CONF-2016-077	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$	0	mono-jet	Yes	3.2	\tilde{t}_1	90-323 GeV $m(\tilde{\chi}_1^0)=m(\tilde{t}_1)=5$ GeV	1604.07773	
	$\tilde{t}_1\tilde{t}_1$ (natural GMSB)	$2 e, \mu$ (Z)	1 b	Yes	20.3	\tilde{t}_1	150-600 GeV $m(\tilde{\chi}_1^0)=150$ GeV	1403.5222	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0 + Z$	$3 e, \mu$ (Z)	1 b	Yes	13.3	\tilde{t}_1	290-700 GeV $m(\tilde{\chi}_1^0)=300$ GeV	ATLAS-CONF-2016-038	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0 + h$	$1 e, \mu$	6 jets + 2 b	Yes	20.3	\tilde{t}_1	320-620 GeV $m(\tilde{\chi}_1^0)=0$ GeV	1506.08616	
	EW direct	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$	$2 e, \mu$	0	Yes	20.3	\tilde{t}_1	90-335 GeV $m(\tilde{\chi}_1^0)=0$ GeV	1403.5294
		$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$	$2 e, \mu$	0	Yes	13.3	\tilde{t}_1	640 GeV $m(\tilde{\chi}_1^0)=0$ GeV, $m(\tilde{\tau})=0.5(m(\tilde{\chi}_1^0)+m(\tilde{t}_1^*))$	ATLAS-CONF-2016-096
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$		2τ	-	Yes	14.8	\tilde{t}_1	580 GeV $m(\tilde{\chi}_1^0)=0$ GeV, $m(\tilde{\tau})=0.5(m(\tilde{\chi}_1^0)+m(\tilde{t}_1^*))$	ATLAS-CONF-2016-093	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$		$3 e, \mu$	0	Yes	13.3	$\tilde{t}_1, \tilde{t}_1^*$	1.0 TeV $m(\tilde{\chi}_1^0)=m(\tilde{t}_1^*), m(\tilde{t}_1^*)=0, m(\tilde{\tau})=0.5(m(\tilde{\chi}_1^0)+m(\tilde{t}_1^*))$	ATLAS-CONF-2016-096	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$		$2-3 e, \mu$	0-2 jets	Yes	20.3	$\tilde{t}_1, \tilde{t}_1^*$	425 GeV $m(\tilde{\chi}_1^0)=m(\tilde{t}_1^*), m(\tilde{t}_1^*)=0, \tilde{t}$ decoupled	1403.5294, 1402.7029	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$		e, μ, γ	0-2 b	Yes	20.3	$\tilde{t}_1, \tilde{t}_1^*$	270 GeV $m(\tilde{\chi}_1^0)=m(\tilde{t}_1^*), m(\tilde{t}_1^*)=0, \tilde{t}$ decoupled	1501.07110	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$		$4 e, \mu$	0	Yes	20.3	$\tilde{t}_1, \tilde{t}_1^*$	635 GeV $m(\tilde{\chi}_1^0)=m(\tilde{t}_1^*), m(\tilde{t}_1^*)=0, m(\tilde{\tau})=0.5(m(\tilde{\chi}_1^0)+m(\tilde{t}_1^*))$	1405.5086	
GGM (wino NLSP) weak prod.		$1 e, \mu + \gamma$	-	Yes	20.3	\tilde{W}	115-370 GeV $c < 1$ mm	1507.05493	
GGM (bino NLSP) weak prod.		2γ	-	Yes	20.3	\tilde{W}	590 GeV $c < 1$ mm	1507.05493	
Long-lived particles		Direct $\tilde{t}_1\tilde{t}_1, \tilde{t}_1$ prod., long-lived \tilde{t}_1^*	Disapp. trk	1 jet	Yes	20.3	\tilde{t}_1^*	270 GeV $m(\tilde{t}_1^*)=m(\tilde{t}_1^*)=160$ MeV, $\tau(\tilde{t}_1^*)=0.2$ ns	1310.3675
		Direct $\tilde{t}_1\tilde{t}_1, \tilde{t}_1$ prod., long-lived \tilde{t}_1^*	dE/dx trk	-	Yes	18.4	\tilde{t}_1^*	495 GeV $m(\tilde{t}_1^*)=m(\tilde{t}_1^*)=160$ MeV, $\tau(\tilde{t}_1^*) < 15$ ns	1506.05332
		Stable, stopped \tilde{g} R-hadron	0-1.5 jets	Yes	27.9	\tilde{g}	850 GeV $m(\tilde{g})=100$ GeV, $10 \mu\text{s} < \tau(\tilde{g}) < 1000$ s	1310.6584	
	Stable \tilde{g} R-hadron	trk	-	3.2	\tilde{g}	1.58 TeV $m(\tilde{g})=100$ GeV, $\tau > 10$ ns	1606.05129		
	Metastable \tilde{g} R-hadron	dE/dx trk	-	3.2	\tilde{g}	1.57 TeV $m(\tilde{g})=100$ GeV, $\tau > 10$ ns	1604.04520		
	GMSB, stable $\tilde{g}, \tilde{t}_1^* \rightarrow t\tilde{\chi}_1^0$	$1-2 \mu$	-	Yes	19.1	\tilde{t}_1^*	537 GeV $1 < \tau(\tilde{t}_1^*) < 3$ ns, SP5B model	1411.6759	
	GMSB, $\tilde{t}_1^* \rightarrow t\tilde{\chi}_1^0$, long-lived \tilde{t}_1^*	2γ	-	Yes	20.3	\tilde{t}_1^*	440 GeV $7 < \tau(\tilde{t}_1^*) < 740$ nm, $m(\tilde{g})=1.3$ TeV	1409.5542	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{g}/\tilde{g}\tilde{g}$	displ. $e\ell/\mu\mu$	-	-	20.3	\tilde{g}	1.0 TeV $6 < c\tau(\tilde{g}) < 480$ nm, $m(\tilde{g})=1.1$ TeV	1504.05162	
	GGM $\tilde{g}, \tilde{g} \rightarrow Z\tilde{g}$	displ. vtx + jets	-	-	20.3	\tilde{g}	1.0 TeV	1504.05162	
	RPV	LFV $pp \rightarrow \tilde{t}_1 + X, \tilde{t}_1 \rightarrow q\bar{q}\tau/\mu$	$e\mu, e\tau, \mu\tau$	-	-	3.2	\tilde{t}_1	1.9 TeV $\tilde{A}_{212} = -0.11, \Delta_{1213} = 0.07$	1607.08079
		Bilinear RPV CMSSM	$2 e, \mu$ (SS)	0-3 b	Yes	20.3	\tilde{g}, \tilde{g}	1.45 TeV $m(\tilde{g})=m(\tilde{g})=400$ GeV, $\tau_{\tilde{t}_1} < 1$ mm	1404.2500
		$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$	$e, \mu, \nu\tau, e\mu, \mu\nu$	-	Yes	13.3	\tilde{t}_1	1.14 TeV $m(\tilde{\chi}_1^0)=480$ GeV, $A_{1230}=0$ ($k=1, 2$)	ATLAS-CONF-2016-075
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\tilde{\chi}_1^0$		$3 e, \mu + \tau$	-	Yes	20.3	\tilde{t}_1	450 GeV $m(\tilde{\chi}_1^0)=0.2, m(\tilde{t}_1^*)=0, A_{1110}=0$	1405.5086	
$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{g}$		0	4-5 large-R jets	-	14.8	\tilde{g}	1.08 TeV $BR(\tilde{g}) \rightarrow BR(b) + BR(s) > 0\%$	ATLAS-CONF-2016-057	
$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\tilde{g}, \tilde{t}_1^* \rightarrow q\bar{q}\tilde{g}$		0	4-5 large-R jets	-	14.8	\tilde{g}	1.55 TeV $m(\tilde{g})=800$ GeV	ATLAS-CONF-2016-057	
$\tilde{g}, \tilde{g} \rightarrow t\bar{t}\tilde{g}, \tilde{t}_1^* \rightarrow q\bar{q}\tilde{g}$		$1 e, \mu$	8-10 jets/0-4 b	-	14.8	\tilde{g}	1.75 TeV $m(\tilde{g})=700$ GeV	ATLAS-CONF-2016-094	
$\tilde{g}, \tilde{g} \rightarrow t\bar{t}\tilde{g}, \tilde{t}_1^* \rightarrow q\bar{q}\tilde{g}$		$1 e, \mu$	8-10 jets/0-4 b	-	14.8	\tilde{g}	1.4 TeV 625 GeV $m(\tilde{g})=850$ GeV	ATLAS-CONF-2016-094	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\tilde{\chi}_1^0$		$2 e, \mu$	2 jets + 2 b	-	15.4	\tilde{t}_1	410 GeV $BR(\tilde{t}_1 \rightarrow b\tilde{\chi}_1^0) > 20\%$	ATLAS-CONF-2016-022, ATLAS-CONF-2016-084	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\tilde{\chi}_1^0$		$2 e, \mu$	2 b	-	20.3	\tilde{t}_1	450-510 GeV $0.4-1.0$ TeV	ATLAS-CONF-2016-022, ATLAS-CONF-2016-084	
Other		Scalar charm, $\tilde{c} \rightarrow c\tilde{\chi}_1^0$	0	$2 c$	Yes	20.3	\tilde{c}	510 GeV $m(\tilde{\chi}_1^0)=200$ GeV	1501.01325

*Only a selection of the available mass limits on new states or phenomena is shown.



Inflation from the SUSY breaking sector

I.A.-Chatrabhuti-Isono-Knoops '16

Can the dilaton be the inflaton in the simple model of SUSY breaking based on a gauged shift symmetry?

the only physical scalar left over, partner (partly) of the goldstino
partly because of a D-term auxiliary component

Same potential cannot satisfy the slow roll condition $|\eta| = |V''/V| \ll 1$ with the dilaton rolling towards the Standard Model minimum

\Rightarrow need to create an appropriate plateau around the maximum of V [10]
without destroying the properties of the SM minimum

\Rightarrow study possible corrections to the Kähler potential
only possibility compatible with the gauged shift symmetry

Extensions of the SUSY breaking model

Parametrize the general **correction** to the Kähler potential:

$$K = -p\kappa^{-2} \log \left(s + \bar{s} + \frac{\xi}{b} F(s + \bar{s}) \right) + \kappa^{-2} b(s + \bar{s})$$
$$W = \kappa^{-3} a, \quad f(s) = \gamma + \beta s$$
$$\mathcal{P} = \kappa^{-2} c \left(b - p \frac{1 + \frac{\xi}{b} F'}{s + \bar{s} + \frac{\xi}{b} F} \right)$$

Three types of possible corrections:

- perturbative: $F \sim (s + \bar{s})^{-n}$, $n \geq 0$
- non-perturbative D-brane instantons: $F \sim e^{-\delta(s+\bar{s})}$, $\delta > 0$
- non-perturbative NS5-brane instantons: $F \sim e^{-\delta(s+\bar{s})^2}$, $\delta > 0$

Only the last can lead to slow-roll conditions with sufficient inflation

Slow-roll inflation

$F = \xi e^{\alpha b^2 \phi^2}$ with $\phi = s + \bar{s} = 1/l \Rightarrow$ two extra parameters $\alpha < 0$, ξ
they control the shape of the potential

slow-roll conditions: $\epsilon = 1/2(V'/V)^2 \ll 1$, $|\eta| = |V''/V| \ll 1$

\Rightarrow allowed regions of the parameter space with $|\xi|$ small

additional independent parameters: a, c, b

SM minimum with tuneable cosmological constant Λ : $V' = 0$, $V = \Lambda \approx 0$

$\xi = 0 \Rightarrow b\phi_{min} = \rho_0$, $\frac{a^2}{bc^2} = \lambda_0$ with ρ_0, λ_0 calculable constants [9]

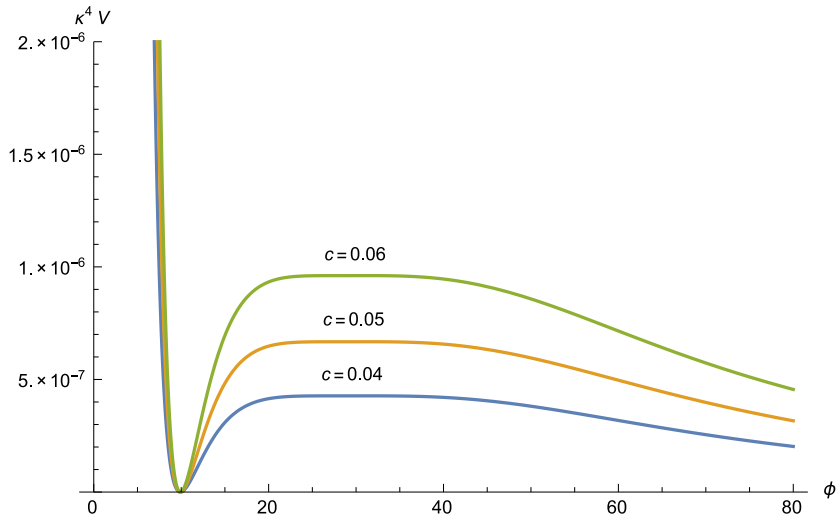
b controls $\phi_{min} \sim 1/g_s$ choose it of order 10

tuning determines a in terms of c overall scale of the potential

$\xi \neq 0 \Rightarrow \rho_0, \lambda_0$ become functions $I(\xi, \alpha), \lambda(\xi, \alpha)$

numerical analysis \Rightarrow mild dependence

$$\xi = 0.025, \alpha = -4.8, p = 2, b = -0.018$$



Fit Planck '15 data and predictions

inflation starts with an initial condition for $\phi = \phi_*$ near the maximum and ends when $|\eta| = 1$

$$\Rightarrow \text{number of e-folds } N = \int_{end}^{start} \frac{V}{V'} d\phi$$

Predictions for the power spectrum of perturbations in CMB:

$$\text{amplitude of density perturbations } A_s = \frac{\kappa^4 \mathcal{V}_*}{24\pi^2 \epsilon_*}$$

$$\text{spectral index } n_s = 1 + 2\eta_* - 6\epsilon_*$$

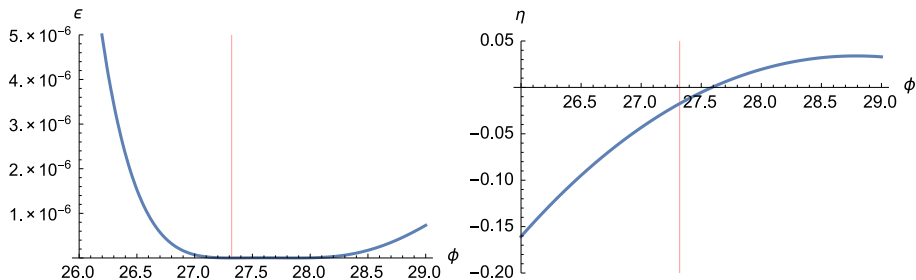
$$\text{tensor - to - scalar ratio } r = 16\epsilon_*$$

Numerical analysis: fit Planck '15 data and keep the SM minimum with an infinitesimal cosmological constant

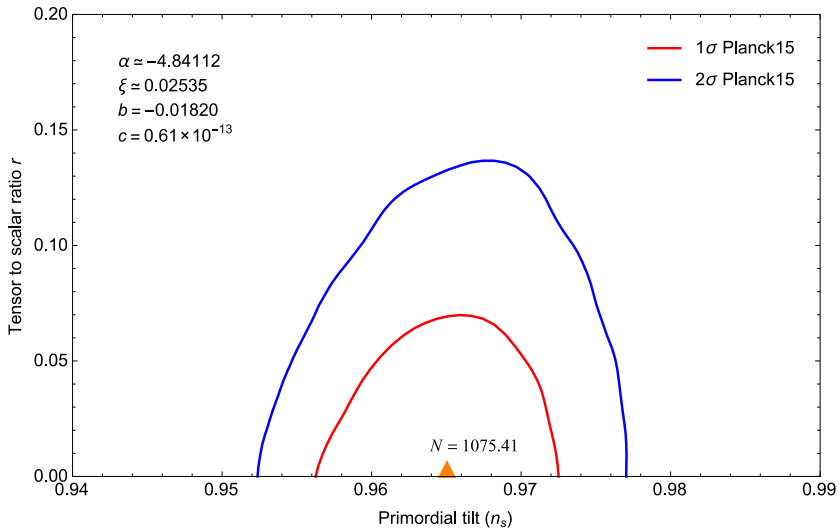
\Rightarrow fine tuning of the parameters of the model

Fit Planck '15 data and predictions

$$p = 2, \phi_* = 27.32, \xi = 0.025, \alpha = -4.8, b = -0.018, c = 0.61 \times 10^{-13}$$



N	n_s	r	A_s
1075	0.965	3×10^{-23}	2.259×10^{-9}



$p = 1$: similar analysis \Rightarrow

$$\phi_* = 64.53, \xi = 0.30, \alpha = -0.78, b = -0.023, c = 10^{-13}$$

N	n_s	r	A_s
889	0.959	4×10^{-22}	2.205×10^{-9}

SM minimum: $\langle \phi \rangle \approx 21.53$, $\langle m_{3/2} \rangle = 18.36$ TeV, $\langle M_{A_\mu} \rangle = 36.18$ TeV

During inflation:

$$H_* = \kappa \sqrt{\mathcal{V}_*/3} = 5.09 \text{ TeV}, m_{3/2}^* = 4.72 \text{ TeV}, M_{A_\mu}^* = 6.78 \text{ TeV}$$

Low energy spectrum essentially the same with $\xi = 0$:

$$m_0^2 = m_{3/2}^2 [-2 + \mathcal{C}], \quad A_0 = m_{3/2} \mathcal{C}, \quad B_0 = A_0 - m_{3/2}$$

$\mathcal{C} = 1.53$ vs at $\xi = 0$: $\mathcal{C}_0 = 1.52$, $m_{3/2}^0 = 17.27$, although $\langle \phi \rangle_0 \approx 9.96$ [6] [28]

Non-linear supersymmetry \Rightarrow goldstino mode χ

Volkov-Akulov '73

Effective field theory of SUSY breaking at low energies

Analog of non-linear σ -model \Rightarrow constraint superfields

Rocek-Tseytlin '78, Lindstrom-Rocek '79, Komargodski-Seiberg '09

Goldstino: chiral superfield X_{NL} satisfying $X_{NL}^2 = 0 \Rightarrow$

$$\begin{aligned} X_{NL}(y) &= \frac{\chi^2}{2F} + \sqrt{2}\theta\chi + \theta^2 F & y^\mu &= x^\mu + i\theta\sigma^\mu\bar{\theta} \\ &= F\Theta^2 & \Theta &= \theta + \frac{\chi}{\sqrt{2}F} \end{aligned}$$

$$\mathcal{L}_{NL} = \int d^4\theta X_{NL}\bar{X}_{NL} - \frac{1}{\sqrt{2}\kappa} \left\{ \int d^2\theta X_{NL} + h.c. \right\} = \mathcal{L}_{\text{Volkov-Akulov}}$$


$$F = \frac{1}{\sqrt{2}\kappa} + \dots$$

Non-linear SUSY in supergravity

I.A.-Dudas-Ferrara-Sagnotti '14

$$K = -3 \log(1 - X\bar{X}) \equiv 3X\bar{X} \quad ; \quad W = fX + W_0 \quad X \equiv X_{NL}$$

$$\Rightarrow \quad V = \frac{1}{3}|f|^2 - 3|W_0|^2 \quad ; \quad m_{3/2}^2 = |W_0|^2$$

- V can have any sign **contrary to global NL SUSY**
- NL SUSY in flat space $\Rightarrow f = 3 m_{3/2} M_p$
- R-symmetry is broken by W_0
- Dual gravitational formulation: $(\mathcal{R} - 6W_0)^2 = 0$ **I.A.-Markou '15**
 **chiral curvature superfield**
- Minimal SUSY extension of R^2 gravity

Starobinsky model of inflation

$$\mathcal{L} = \frac{1}{2}R + \alpha R^2$$

$$\text{Lagrange multiplier } \phi \Rightarrow \mathcal{L} = \frac{1}{2}(1 + 2\phi)R - \frac{1}{4\alpha}\phi^2$$

Weyl rescaling \Rightarrow equivalent to a scalar field with exponential potential:

$$\mathcal{L} = \frac{1}{2}R - \frac{1}{2}(\partial\phi)^2 - \frac{M^2}{12} \left(1 - e^{-\sqrt{\frac{2}{3}}\phi}\right)^2 \quad M^2 = \frac{3}{4\alpha}$$

Note that the two metrics are not the same

supersymmetric extension:

add D-term $\mathcal{R}\bar{\mathcal{R}}$ because F-term \mathcal{R}^2 does not contain R^2

\Rightarrow brings two chiral multiplets

SUSY extension of Starobinsky model

$$K = -3 \ln(T + \bar{T} - C\bar{C}) \quad ; \quad W = MC(T - \frac{1}{2})$$

- T contains the inflaton: $\text{Re } T = e^{\sqrt{\frac{2}{3}}\phi}$
- $C \sim \mathcal{R}$ is unstable during inflation

⇒ add higher order terms to stabilize it

e.g. $C\bar{C} \rightarrow h(C, \bar{C}) = C\bar{C} - \zeta(C\bar{C})^2$ Kallosh-Linde '13

- SUSY is broken during inflation with C the goldstino superfield

→ model independent treatment in the decoupling sgoldstino limit

⇒ minimal SUSY extension that evades stability problem

Non-linear Starobinsky supergravity

$$K = -3 \ln(T + \bar{T} - X\bar{X}) \quad ; \quad W = MXT + fX + W_0 \quad \Rightarrow$$

$$\mathcal{L} = \frac{1}{2}R - \frac{1}{2}(\partial\phi)^2 - \frac{M^2}{12} \left(1 - e^{-\sqrt{\frac{2}{3}}\phi}\right)^2 - \frac{1}{2}e^{-2\sqrt{\frac{2}{3}}\phi}(\partial a)^2 - \frac{M^2}{18}e^{-2\sqrt{\frac{2}{3}}\phi}a^2$$

- axion a much heavier than ϕ during inflation, decouples:

$$m_\phi = \frac{M}{3}e^{-\sqrt{\frac{2}{3}}\phi_0} \ll m_a = \frac{M}{3}$$

- inflation scale M independent from NL-SUSY breaking scale f

\Rightarrow compatible with low energy SUSY

- however inflaton different from goldstino superpartner
- also initial conditions require trans-planckian values for ϕ ($\phi > 1$)

Conclusions

String phenomenology:

Consistent framework for particle physics and cosmology

Challenge of scales: at least three very different (besides M_{Planck})
electroweak, dark energy, inflation, SUSY?

their origins may be connected or independent

SUSY with infinitesimal (tuneable) +ve cosmological constant

- interesting framework for model building incorporating dark energy
- identify inflaton with goldstino superpartner
inflation at the SUSY breaking scale (TeV?)